

St. Patrick's High School, Keady Mathematics Department

GCSE Mathematics Practice Booklet

M6 Topic I – Number I

Ratio

Estimations

Binary

<u>Section A – Non Calculator Questions / Mark Scheme Pages 1-22</u> <u>Section B – Calculator Questions / Mark Scheme Pages 23 - 39</u>

Questions taken from CCEA Past Papers



Q1 Estimate
$$\frac{604 \times 2.91}{7.9 - 3.76}$$

Show all your working.

Answer _____ [2]

Q2 (a) Estimate the total weight of 69 pies weighing 102 g each.

Answer _____ g [1]

(b) Estimate the greatest number of pencils costing 39p each that can be bought with £20

Answer _____ [2]

Q3 (a) There are 6 eggs in each egg box.

Estimate the total number of boxes needed to pack 297 eggs.

Answer _____ [2]

(b) Tommy earns £6.15 per hour.

Estimate his earnings for 39 hours.

Answer £ _____ [2]

Q4 A rectangular room measures 475 cm by 295 cm. Estimate the number of square tiles of side 32 cm needed to tile the floor. Show all your working clearly.

	295 cm	32 cm
475 cm		

Answer _____ [3]

- Q5 A manager wishes to buy new uniforms for his 30 staff. A shirt costs £8.15 and trousers cost £19.95
 - (a) Estimate the total cost of the uniforms. Show all steps of your working clearly.

Answer £ _____ [2]

(b) Without any further calculation, decide whether your estimate will be an overestimate or an underestimate of the exact cost.
 Explain your reasoning clearly.

_____ [2]

Q6 Amy, Katie and Maria use their calculators to work out the value of

$\frac{27.98}{4.27\times0.48}$

Amy gets 3.145, Katie gets 136.51 and Maria gets 13.651

Use approximations to show which one of them is correct.

You must show all your working.

Q7 Explain why $\sqrt{73}$ must be a number between 8 and 9

[2]

Q8 Estimate the value of 98×6.9

You must show your work.

Answer _____ [2]

Q9 (a) Estimate the cost of 31 books at £8.85 each.

Answer £ _____ [1]

(b) Estimate how many 18.5 cm lengths of tape can be cut from 1500 cm.

Answer [1]

Q10 A sheet of paper is 300 mm long and 210 mm wide.

Find in its simplest form the ratio of the length of the sheet to the width of the sheet.

Answer _____ [2]

Q11 (a) Lucy has a bag containing only 5p and 20p coins.

The ratio of the number of 5p coins to the number of 20p coins is 5 : 4

Work out the ratio of the total value of the 5p coins to the total value of the 20p coins.

Give your answer in its simplest form.

Answer _____ [2]

(b) John and Mark share an amount of money in the ratio 5 : 6

Mark's share is £48

What was the total amount shared?

Answer £_____ [2]

Q12 Here is a recipe for making some scones.

Self-raising flour	340 g
Caster sugar	55 g
Butter	85 g
Milk	125 ml
Natural yoghurt	60 ml

Linda has only 100 ml of milk.

Complete the table to show how much of the other ingredients she needs.

Self-raising flour	g
Caster sugar	g
Butter	g
Milk	100 ml
Natural yoghurt	ml

Q13 The prize money in a golf tournament is divided between the three golfers who finish first, second and third in the ratio 7 : 4 : 3

What **fraction** of the prize money does each of the first three golfers receive?

Write each fraction in its simplest form.

 Answer
 1st _____
 2nd _____
 3rd _____
 [3]

Q14 This recipe makes 16 scones with the following ingredients.

Ingredients

- 250 g flour
- 1 tsp baking powder
- 40 g butter
- 25 g sugar
- 1 large egg
- about 100 ml milk



Source: Getty Images 609903116

(a) Paul wants to make 20 scones.

How much butter will he need?

Answer	g [2]
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(b) Paul has 300 g of flour.

Has he enough flour to make 20 scones?

Show all your working.

Answer	because	[2]
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Q15 (a) 60% of entrants pass a test.

What is the ratio of

number who pass : number who fail?

Give your answer in simplest form.

Answer [2]

(b) The ratio of boys : girls born in a hospital one week was 3:5

What fraction were girls?

Answer [1]

Q16 (a) Write 25 as a binary number.

Answer [1]

(b) Write the binary number 1101001 in decimal form.

Answer _____ [1]

Q17 (a) Write the binary number 10101 as a decimal number.

Answer [1]

(b) Write the decimal number 26 as a binary number.

Answer [1]

 Q18
 (a) What is the main difference between the Binary number system and the Decimal number system?

 Answer ________[1]
 (b) Write the binary number 111111 as a decimal number.

 (b) Write the binary number 111111 as a decimal number.
 [1]

 (c) Write the decimal number 87 as a binary number.
 [1]

 Answer ______[1]
 [1]

Q19	110110 is a binary number.
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20 is a decimal number.

Work out the total of the two numbers.

Give your answer as a binary number.

Answer [3]

Q20 (a) Write the decimal number 15 as a binary number.

Answer _____ [1]

(b) Write the binary number 1000000 as a decimal number.

Answer _____ [1]

1.
$$\frac{600 \times 3}{8-4}$$
 or $\frac{604 \times 3}{8-4}$ MA1
 $\frac{1800}{4} = 450$ or $\frac{1812}{4} = 453$ A1

2.	(a) 7000	A1
	(b) $2000 \div 40 = 50$	M1 A1

3. (a)
$$\frac{300}{6} = 50$$
 M1 A1
(b) $6 \times 40 = \pounds 240$ M1 A1

4.	$\frac{480}{30} = 16$	MA1
	$\frac{300}{30} = 10$	MA1
	$16 \times 10 = 160$	MA1
	or	
	$480 \times 300 = 144000$	MA1
	$30 \times 30 = 900$	MA1
	$\frac{144000}{900} = 160$	MA1

5.	(a)	$30 \times 8 + 30 \times 20$ = 240 + 600	MA1	
		= 840	A1	
	(b)	Underestimate because 30×15 rounded down for shirts and only 30×5 pence rounded up for trousers; so overall effect will be lower than actual cost (or similar explanation)	A2	
	or			
	(a)	$30 \times (8 + 20) = 30 \times 28 = (30 \times 30) = 900$	MA1 A1	
	(b)	Overestimate because total of shirt and trousers rounded up; so overall effect will be higher than the actual cost (or similar explanation)	A2	

6.	$\frac{30}{4 \times 0.5}$ or $\frac{28}{4 \times 0.5}$	C1
	$\frac{30}{12} = 15$ or $\frac{28}{2} = 14$	C1
	This is closest to 13.651 so Maria is correct	C1

7.	$8^2 = 64$ and $9^2 = 81$	C1
	73 lies between 64 and 81	C1
8.	100×7	M1

8.	100 × 7 700	M1 A1
9.	(a) 270	A1
	(b) 75	A1

10.	300 : 210 = 10 : 7	A1 A1	
	= 10 : 7	Al	

11.	(a)	25:80	MA1	
		5:16	A1	
	(b)	$48 \div 6 = 8$	MA1	
		$11 \times 8 = 88$	A1	

12. 272 44 68

48

A3

13.

Using	g 14		A1
$\frac{1}{2}$	$\frac{2}{7}$	$\frac{3}{14}$	A2

(A1 for 2 correct or $\frac{7}{14}$, $\frac{4}{14}$, $\frac{3}{14}$)

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14.	(a)	$40 \div 4 \times 5 = 50 \mathrm{g}$	M1 A1	
	(b)	$250 \div 4 = 62.5 \qquad 62.5 \times 5 = 312.5$	MA1	
		No because he needs 12.5 g more (or at least 310 or $\frac{1}{4}$ of 250g is more than 50g) or equivalent	A1	
15.				
10.	(a)	60:40 ans 3:2	A1 A1	
	(b)	$\frac{5}{8}$	A1	
16.	(a)	11001	A1	
	(b)	105	A1	
17.	(a)	21	A1	
	(b)	11010	A1	

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18.	(a)	Base 2 rather than base 10	or	Binary system uses only 2 symbols	A1
	(b)	63			A1
	(c)	1010111			A1

19.

110110 = 54	A1
54 + 20 = 74	A1
74 = 1001010	A1

20.

(a) 1111	A1
(b) 64	A1

250 g Dark Chocolate

100 g Butter

120 g Caster Sugar

150 ml Water

3 Eggs

500 ml Double Cream

This ice cream recipe will serve 4 people.

(a) How much caster sugar is needed in a recipe for 7 people?

Answer _____ g [2]

(b) Liz has 13 eggs and needs to make chocolate ice cream for 17 people.

Does she have enough eggs? Explain your answer.

Q2 The exchange rate between pounds and euro is $\pounds 1 = \pounds 1.35$

Sam buys a coat for €108

How much does the coat cost in (£) pounds?

Answer £ ____ [2]

Q3 Philip rents a holiday home in Florida in May. It costs him £680 Dave rents the same home in August for \$1400 Given $\pounds 1 = \$1.52$ how much **more** does Dave pay in \pounds for the holiday home?

Answer £ _____ [4]

(a) The teacher to pupil ratio in a school is 1:15 There are 960 pupils in the school. How many teachers are there?

Q4

Answer _____ [2]

(b) 418 of these pupils play football, netball or hockey in the ratio 11:3:8 How many pupils play netball?

Answer _____ [3]

Q5 Here is a recipe for making some scones.

Self-raising flour	340 g
Caster sugar	55 g
Butter	85 g
Milk	125 ml
Natural yoghurt	60 ml

Linda has only 100 ml of milk.

Complete the table to show how much of the other ingredients she needs.

Self-raising flour	g
Caster sugar	g
Butter	g
Milk	100 ml
Natural yoghurt	ml

Q6 Marie is booking a cruise holiday. She is offered a discount of €140 or she can have \$200 to spend on board her cruise.

Use the exchange rates below to work out which is the better offer, \notin 140 or \$200

 $\pounds 1 = \pounds 1.19$ $\pounds 1 = \$ 1.67$

You must show working to justify your answer.

Answer _____ [3]

Q7 Andrew, Karan and Caroline share £33.60 in the ratio 5 : 4 : 3

Work out how much money they each receive.

Answer Andrew £_____

Karan £_____

Caroline £ [3]

(a) In a choir there are 36 female and 24 male singers.

Q8

Write down the ratio of female to male singers in its simplest form.

Answer [2]

(b) There are 52 people in an orchestra. The ratio of males to females is 3:1 Calculate the number of males and females in the orchestra.

Answer _____ males, _____ females [2]

Q9 Orange juice is mixed with water in the ratio 1:11 (orange juice:water). How much orange juice and how much water make up 3 litres in total?

Give your answers in ml.

Answer Orange juice _____ ml

Water _____ ml

Q10 Marie has a recipe for Spaghetti Carbonara which requires the following ingredients.

Spaghetti	500 g
Bacon	200 g
Eggs	8
Cream	76 ml
Parmesan	48 g

Marie only has 150 g of bacon.

Work out how much of the other ingredients she should use.

Spaghetti	g
Eggs	
Cream	ml
Parmesan	g

[3]



It takes 2 days to paint the outside of 6 houses.

(a) How long would it take to paint the outside of 15 houses?

<u> </u>
[1]
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Q12 (a) Write 25 as a binary number.

Answer [1]

(b) Write the binary number 1101001 in decimal form.

Answer _____ [1]

Q13 Write the binary number 1011001 as a decimal number.

Answer [1]

Q14 (a) Write the decimal number 19 as a binary number.

Answer [1]

(b) Rearrange h - 3m = y to make *m* the subject.

Answer [2]

1.	(a) $120 \div 4 \times 7 = 210 \text{ g}$	M1 A1
	(b) $\frac{3}{4} \times 17 = 12.75$ therefore she has enough eggs	C2

2.	108 ÷ 1.35	M1
	80	A1

3.	$1400 \div 1.52 = \pounds 921.05$	M1 A1
	$921.05 - 680 = \pounds 241.05$	M1 A1

4.	(a)	$960 \div 15 = 64$	M1 A1	
	(b)	$418 \div 22$ 19 $3 \times 19 = 57$	M1 A1 MA1	

5.	272	
	272 44	
	68 48	
	48	A3

6.		
0.	€140 = £117.647	MA1
	200 = £119.76	MA1
	\$200 is worth more	A1

7.	14.00 11.20 8.40	A1 A1 A1

8.	(a) 36:24 3:2	A1 A1
	(b) 39, 13	A1 A1

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9.	Using $\frac{1}{12}$	M1	
	250, 2750	A1 A1	

10.

Spaghetti	375g
Eggs	6
Cream	57ml
Parmesan	36g

All correct (A2 for 3 correct, A1 for 2 correct) A3

11.

(a) $15 \div 6 \times 2 = 5$	M1A1
(b) all painters work at the same rate or houses are the same size	A1

12.	(a) 11001	A1
	(b) 105	A1

64	32	16	8	4	2	1
1	0	1	1	0	0	1

MA1

A1

= 64 + 16 + 8 + 1= 89 (correct answer, with no work shown, gains mark)

14. (a) 10011

(b)
$$h-y=3m$$
 MA1
 $m=\frac{h-y}{3}$ A1