

## St. Patrick's High School, Keady Mathematics Department

#### **GCSE Mathematics Practice Booklet**

### **M6**

# Topic 7 – Handling Data 1 - Probability

Listing Outcomes
Probability Scale
Calculating Probabilities
Expectation
Relative Frequency

Section A – Non Calculator Questions / Mark Scheme Pages 1-52

Section B – Calculator Questions / Mark Scheme Pages 53-80

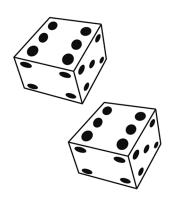
Questions taken from CCEA Past Papers



# Q1 To start a game, Darragh must score **a total** of either 2 or 5 or 7 from throwing two fair dice.

(a) Complete the table to show all the possible totals.

+	1	2	3	<ul><li>4</li><li>5</li><li>6</li></ul>	5	6
1	2	3	4	5	6	7
2	3	4	5	6	7	8
3	4	5				
4	5	6				
5	6	7				
6	7	8				



[2]

**(b)** What is the probability of Darragh getting started straight away?

Answer \_\_\_\_\_ [2]

<b>Q2</b>	A three-sided spinner has the numbers 2, 4 and 6 written on it. The probability of
	getting each number is the same.

A fair dice has the numbers 1, 3, 5, 7, 9 and 11 written on it.

In a game the spinner is spun and the dice is rolled. The two scores are added together.

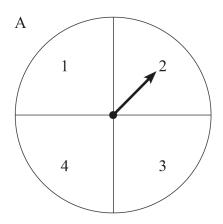
(a) Use the two-way table to show all the outcomes for the sum of the two scores.

+	1	3	5	7	9	11
2						
4						
6						

[2]

<b>(b)</b>	What is the	probability th	at the sum	of the two	scores is	greater than	123
------------	-------------	----------------	------------	------------	-----------	--------------	-----

Answer	[2]
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B 2

Spinners A and B are each spun once.

(a) Complete the table to show all the possible outcomes.

		Spinner B						
_		1	2	3				
Spinner A	1 2 3 4	1, 1 2, 1 3, 1	1, 2 2, 2	1, 3				
Sp	3		- <b>, -</b>					

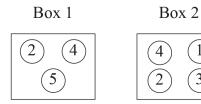
[1]

**(b)** What is the probability of getting the same number on each spinner?

Answer \_\_\_\_\_ [1]

(c) What is the probability of getting a bigger number on A than B?

Answer \_\_\_\_\_[1]



There are two boxes of counters.

Each counter has a number on it as shown.

Mike takes one counter at random from Box 1 and then one counter at random from Box 2  $\,$ 

(a) Complete the table to show all possible outcomes of counters taken.

		Box 2				
		1	2	3	4	
	2	(2, 1)	(2, 2)			
Box 1	4	(4, 1)				
	5					[2]

**(b)** What is the probability that Mike takes a counter with the same number on it from each box?

Answer \_\_\_\_\_ [1]

	The numbers on the counters taken are <b>multiplied</b> .
	What is the probability of this multiplication giving an <b>even</b> number?
	Answer
(d)	On another day, Laura takes one counter from each box and <b>multiplies</b> the numbers together.
	She replaces the counters and does the same thing again for a total of 30 times.
	How many times would you expect her to get an odd number answer?
	Answer

(a) The probability that Matt eats breakfast is marked on the scale with a B.

What is the probability?



Answer	[1]	
AIISWCI	1	

(b) Matt has a three-digit combination lock for his bike.



He has forgotten the code.

He knows the first digit is 2

The second digit is either 3 or 4

The third digit is 5, 6 or 7

List all the possible combinations of Matt's code.

<b>Q6</b>	A bag contains	five counters.	each one a	different o	colour
_		II TO COMITTOID,	outil one a	WILL OI OILL C	Oloui

The colours are red (R), green (G), blue (B), white (W) and yellow (Y).

Daniel takes a counter at random from the bag.

Daniel now tosses a fair coin.

One possible outcome is (red, heads), which can be written as (R, H).

(a) List all the possible outcomes for this experiment in this way in the two-way table below.

One has already been done for you.

**Counter (colour)** 

		R	G	В	W	Y
Coin	Н	(R, H)				
Coin	Т					

[2]

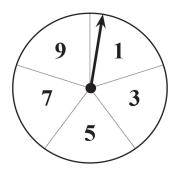
**(b)** What is the probability that the outcome is (B, H)?

Answer \_\_\_\_\_ [1]

(c) What is the probability that the outcome of this experiment contains a green (G) or a tail (T) or both of these?

Answer [2]

Q7 A fair spinner has outcomes of 1, 3, 5, 7 and 9



The spinner is spun twice.

The two outcomes are added together to give a score.

(a) Complete the table below to show all possible scores.

First spin

Second spin

+	1	3	5	7	9
1	2				
3		6			
5			10		
7	8			14	
9			14		18

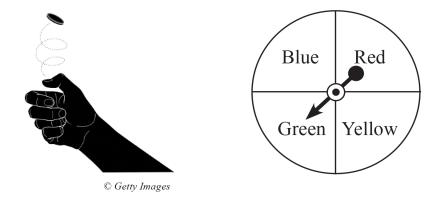
[2]

**(b)** What is the probability of getting the "most likely" score?

Answer\_\_\_\_\_ [1]

Q8 Bill flips a fair coin with outcomes head and tail once.

He spins the spinner with outcomes blue, red, yellow and green once.



(a) List all the possible outcomes that Bill can get.

[2]

(b) The probability of getting an outcome of a tail and yellow is  $\frac{1}{8}$  Explain clearly why this is the case.

[1]

- Q9 Kendra flips a coin and rolls a dice.
  - (a) List all the possible outcomes in the table below.

Two have already been filled in for you.

			I	Dice			
		1	2	3	4	5	6
Coin	Heads (H)	H1					
	Tails (T)					T5	

Given that each outcome is equally likely, find the probability that

(b) Kendra gets a 5,

		Answer	[1]
(c)	Kendra gets a Tail and an odd number.		
		Answer	[1]

[2]

Q10 Below is a menu from Dillies Diner.

A two-course lunch is made up of one Starter and one Main course.

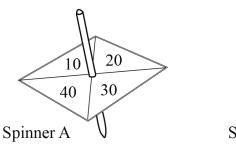
### **DILLIES DINER LUNCH MENU**

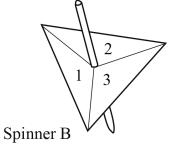
Starter	Main Course
Soup Mushrooms Ribs	Plaice Beef Chicken Quiche

Work out the number of different two-course lunches that can be ordered from this menu.

Answer_	_lunches [2]

Q11 Two fair spinners are each spun once.





The scores on each spinner are multiplied together.

(a) Complete the table of outcomes.

		Spinner A			
	×	10	20	30	40
	1				
Spinner B	2				
	3				

[2]

**(b)** What is the probability that the outcome is 60?

Answer \_\_\_\_\_ [1]

(c) What is the probability that the outcome is less than 40?

Answer \_\_\_\_\_ [2]

Q12	Cathy can buy either a 16GB memory stick or a 64GB memory stick.  The memory sticks are coloured black, red, yellow or green.					
	(a) Write down the size and colour of all the different memory sticks that can buy.					
		[2]				
	(b) Cathy bought one of each type of memory stick.					
	She gives one to her friend Jill.					
	What is the probability that this is a yellow 16GB memory stick?					
	Answer	[1]				

Q13	Michael tosses a fair coin and rolls a fair 6-sided dice.	
	Work out the probability that the outcome is a head and a three.	
	You must show how you found your answer.	
	Answer	_ [2]
Q14	Two fair dice are rolled.	
	Make a list of all the ways it is possible to get a total score of 7 on the two dice.	
	Answer	[2]

Q15 A fair six-sided dice is rolled once.

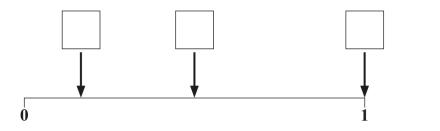


**A**: An even number is rolled.

**B**: A number greater than 0 is rolled.

C: A number less than 2 is rolled.

Label the boxes with the correct letter to show the probability of A, B and C.



[3]

Ben has five flags from Asia.

They are from Malaysia, Mongolia, Myanmar, Taiwan, and Vietnam.

Ben takes one of these flags at random.

(a) Mark on the probability scale with a V the probability that the flag taken is Vietnam.

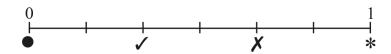


[1]

**(b)** Mark on the probability scale with an **M** the probability that the flag taken is from a country beginning with the letter M.



[1]



One letter is taken at random from the word COMMON.

Which of  $\bullet$ ,  $\checkmark$ , x, \* shows the probability that the letter is

(a) M,

Answer \_\_\_\_ [1]

**(b)** T,

Answer \_\_\_\_ [1]

(c) a letter that appears twice in COMMON,

Answer [1]

(d) a letter in the word MONOCLE?

Answer \_\_\_\_ [1]

Q18 There are twenty balls in a bag.

4 are blue, 6 are green and the rest are white.

A ball is taken at random from the bag.

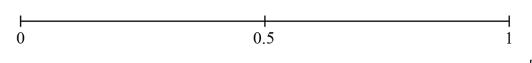
Mark the probability of each of the following events happening on the probability scale below using the capital letters.

- B The ball taken is blue
- W The ball taken is white
- R The ball taken is red



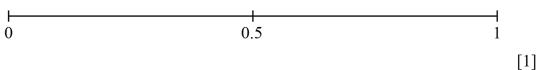
[3]

(a) On the probability scale mark with a cross (X) the probability that it will snow in Belfast in July.

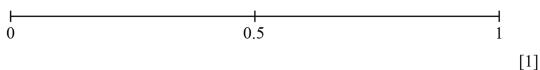


[1]

(b) On the probability scale mark with a cross (X) the probability that it will rain in Belfast next year.



(c) On the probability scale mark with a cross (X) the probability that you will get a tail when you toss a fair coin.



(d) The weather forecaster says that there is a 70% chance of rain tomorrow.

What is the probability that it will not rain tomorrow?

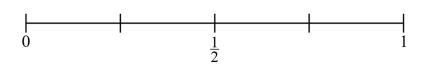
Answer			1	
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(a) A probability scale goes from 0 to 1

What does the number 1 tell you about the chance of an event happening?

[1]

**(b)** Mark with an arrow and the letter P, the probability of having a birthday on 32nd January.



[1]

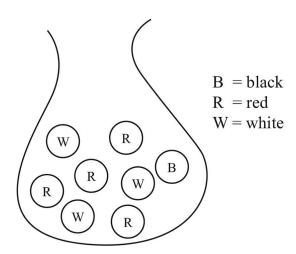
(c) 300 tickets are sold in a school raffle.

Only boys and girls buy tickets.

Explain why the probability of a boy winning may not be  $\frac{1}{2}$ 

[1]

**Q21** A bag contains 1 black, 4 red and 3 white counters.



- (a) Emma takes a counter at random from the bag. On the scale below:
  - (i) mark with an arrow and the letter G, the probability that the counter taken is green, [1]
  - (ii) mark with an arrow and the letter T, the probability that the counter taken is red or white. [2]



(b) Emma replaces the counter in the bag. A number of pink counters are added to the bag. A counter is now taken at random from the bag. The probability that it is red is now  $\frac{1}{5}$ .

How many pink counters were added to the bag?

Answer \_\_\_\_\_\_ [2]

Q22	(a) Lucy says that the probability of her getting a car for her 18th birthday is $\frac{3}{2}$ Explain what is wrong with Lucy's statement.				
	[1]				
	<b>(b)</b> Lucy phones Tom. The probability that the phone line is busy is 0.26				
	What is the probability that it is not busy?				
	Answer[1]				
Q23	The 8 cards shown below are shuffled and placed with the pictures face down on a table.  Megan knows there are two cards with circles and two cards with triangles. She says, "There are an equal number of cards with circles and cards with triangles, so the probability of me taking a card with a triangle is 0.5".  Is Megan correct? Explain your reasoning clearly.				

Q24 There are 2 ham sandwiches, 3 chicken sandwiches, 4 cheese sandwiches and 1 egg sandwich on a plate.

Benny takes a sandwich at random from the plate.



Which point (A, B, C, D, E or F) on the probability scale best matches the probability of Benny taking

(a) a prawn sandwich,

Answer \_\_\_\_\_ [1]

**(b)** a cheese sandwich?

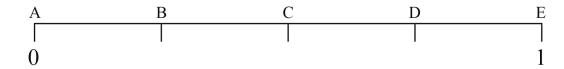
Answer \_\_\_\_\_ [1]

There are 80 packets of crisps in a school tuck shop.

The number of packets of each flavour is shown in the table.

Cheese & Onion	Pickled Onion	Prawn Cocktail	Ready Salted	Salt & Vinegar
20	7	8	5	40

A packet of crisps is chosen at random.



Which letter on the scale shows the probability that the flavour is

(a) Salt & Vinegar,

A	Г1	٦
Answer	L	п

(b) Cheese & Onion,

Answer [1		
	٠.	

(c) Roast Chicken?

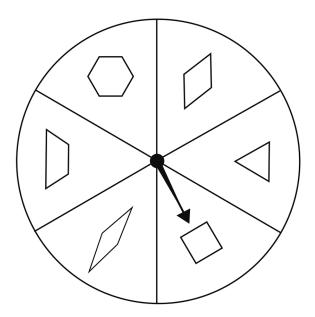
Answer	П

<b>)</b> 26	A bag contains 21 pieces of fudge. 6 pieces are vanilla and 8 pieces are walnut. The rest are raisin. Josh takes a piece of fudge at random from the bag. What is the probability that it is			
	(a) not vanilla,			
		Answer	[1]	
	(b) raisin?			
		Answer	[1]	

Q27 The table shows information about all pupils in a Year 12 class.

	Boys	Girls
Blue Eyes	4	6
Brown Eyes	10	8

Br	own Eyes	10	8	
(a)	How many pupils	s are there in the class	?	
			Answer _	[1]
(b)	A pupil is to be c	hosen at random.		
	What is the proba	ibility that the pupil w	ill have blue eyes?	
			Answer _	[1]
(c)	A pupil was chos	en. It was a boy.		
	What is the proba	ibility that he had brow	wn eyes?	
				ro
			Answer	Γ2



Sara spins a fair spinner with some shapes drawn on it.

What is the probability of Sara getting a shape which

(a) has 4 sides,

Answer \_\_\_\_\_ [1]

**(b)** has less than 3 sides,

Answer \_\_\_\_\_ [1]

(c) has less than 4 sides?

Answer \_\_\_\_\_[1]

<b>Q29</b>	In a raffle all 400 tickets were sold.
Q <sub>2</sub> j	III a fairle all 400 tickets were sold.

The tickets were numbered from 1 to 400

One ticket is to be drawn at random to win the prize.

What is the probability that the winning ticket will be numbered greater than 275?

Answer	[2]
7 1115 VV C1	

Q30 The probability for the number of goals scored in a league match during the season is given in the table below.

Number of goals	0	1	2	3	4	5 or more
Probability	0.15	0.23	0.13	0.28	0.12	0.09

What is the probability of at least 3 goals being scored in a league match?

<b>A</b>	
Answer	

Q31	A box containing 14 pencils has 3 pencils with broken leads.				
	A pencil is taken at random from the box.				
	(a) What is the probability that it does not have a broken	lead?			
		Answer	[2]		
	The pencil taken does not have a broken lead and is not re-	eplaced.			
	<b>(b)</b> What is the probability that the next pencil taken has	a broken lead?			
		Answer	_[1]		

Q32 A bag contains a number of counters.

They are either red, green, black or white.

In the bag the number of black counters is the same as the number of white counters.

The table shows some of the probabilities of taking a counter at random from the bag.

Colour	red	green	black	white
Probability	0.3	0.4		

Teresa takes a counter at random from the bag.

What is the probability that Teresa takes a white counter?

Angreson	ГЭ
Answer	4

233	Tickets numbered from 1 to 81 are placed in a hat. One winning ticket is taken at random.	
	(a) What is the probability that the winning ticket is	the number 70?
		Answer [1]
	<b>(b)</b> What is the probability that the winning ticket is	a number bigger than 70?
		Answer [2]
	(c) Explain why the probability of the winning ticke	t having an even number is not $\frac{1}{2}$
		[1]

<b>U34</b>
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There are 32 pupils in a class and all were present on Monday.

On Monday the teacher asked each pupil their favourite colour.

She recorded the results for green, blue and yellow accurately in a table.

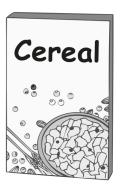
	Green	Blue	Yellow	Total
Girls	3	5	4	12
Boys	4	7	2	13
Total	7	12	6	25

(a)	Give a reason why the total number of boys and girls i	n the table is not 32	[1]
(b)	There are 18 girls in the class.		
	What is the probability that a girl said the colour blue?		<b>[1]</b>
(c)	What is the probability that a pupil in the class <b>did no</b>	Answert say green?	_[1]
		Answer	_[1]

A machine fills boxes of breakfast cereal.

Each box should weigh 375 g.

Jason takes 100 boxes and tests the accuracy of the machine by weighing them.



Weight (g)	Less than 375	Exactly 375	More than 375
Number of boxes	9	58	33

(a)	What is the probability that one of the boxes taken by Jason weighs less
	than 375 g?

Answer \_\_\_\_ [1]

**(b)** The machine fills 5000 boxes.

Calculate the number of boxes you would expect to weigh less than 375 g.

Answer \_\_\_\_\_ [2]

In a Year 12 class, the following information was recorded.

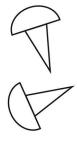
	Boys	Girls
Wears glasses	3	5
Does not wear glasses	10	6

	Does not wear glasses	10	6					
(a) What fraction of the pupils in the class wear glasses?								
				Answer	_[2]			
(b)	(b) A pupil was chosen at random from the class.							
What is the probability that the pupil was a boy who does not wear glasses?								
				Answer	_[1]			
(c)	The next week	a new boy joins th	e class.					
	He wears glasses.							
	Will this change the probability of now choosing at random a girl who wears glasses?							
	Explain your	answer clearly.						
	Answer	because			[2]			

Q37	Marcus wants to investigate the likelihood of a drawing pin landing point up or point
	down when dropped.

He drops a drawing pin a number of times. His results are shown in the table.

up
up
down
up
up
down
up
down



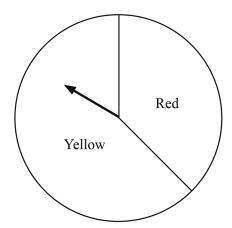
(a) What is the relative frequency of the drawing pin landing point up?

Answer	[1	Ī
101 76 9 10		-

**(b)** Marcus concludes that a drawing pin is more likely to land point up. Comment on his conclusion.

[1]

Q38 A spinner has a red sector and a yellow sector as shown.



The arrow is spun 1000 times.

The table shows the relative frequency of the arrow landing on red after different numbers of spins.

Number of spins	Relative frequency of red
50	0.44
100	0.37
200	0.34
500	0.31
1000	0.32

Answer	[2	2	

<b>(b)</b>	Which relative	frequency	gives th	e best	estimate	of the	probability	of obtai	ining
	a red?								

Explain your answer.

	because	Answer
[3		

Q39 A six-sided dice is rolled 800 times.

The table below shows the relative frequency of scoring a six after different numbers of rolls.

Number of rolls	Relative frequency of a six
100	0.3
200	0.26
300	0.27
500	0.23
800	0.25

(a)	How many times was a six	scored	after 3	300 r	olls?
	Show how you obtained y	our ansv	ver.		

Answer	[2]	

<b>(b)</b>	Which relative frequency from the table gives the best estimate of the probability
	of scoring a six when this dice is rolled?

Explain your answer.

Answer \_\_\_\_\_

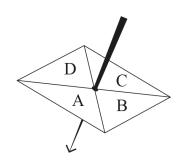
Reason \_\_\_\_\_\_ [2]

(c) How many sixes would you expect to get if a **fair** six-sided dice was rolled 300 times?

Answer [2]

A spinner has sections labelled A, B, C and D.

The spinner is spun, and the relative frequency of landing on D is recorded after every 10 spins.



Some of the results are recorded in the table below.

Number of spins	Relative frequency of D
10	0.5
20	0.3
30	0.4
40	0.35
50	
60	0.45

4	(a)	A ftor	50	anina	tha	spinner	had	landad	on D	10	timas
l	a	Aller	20	Spins	uie	Spinner	Hau	Tanueu	טווט	19	umes.

Fill in the missing relative frequency in the table above.

[1]

(b) How many times had the spinner landed on D after 60 spins?

Answer	- 11

	Angwar							answer.	
	Allswei								
(d)	If the spin on D?	ner is spun	400 times	how m	any time	s woul	d you exp	pect it to	land
						A	Answer _		
Tony	tests a six-s	idad dica x	1 1 1 1			_	.1	1	
Tony	icsis a six s	sided dice	which he t	thinks is	biased	toward	s the eve	n numb	ers.
	rries out an					toward	s the eve	n numb	ers.
Не са		experimen	nt by rollin	ng the d	ice.	toward	s the eve	n numb	ers.
Не са	rries out an	experimen	nt by rollin	ng the d O (odd)	ice.	toward E	s the eve		ers.
He ca	rries out an	experiments as E	nt by rollin (even) or ( O E	ng the d O (odd) E	ice. O E	E			ers.
He ca	rries out an cords the re E	experiments as E	nt by rollin (even) or ( O E	ng the d O (odd) E	ice. O E	E			ers.
He ca	rries out an cords the re E	experiments as E	nt by rollin (even) or ( O E	ng the d O (odd) E	ice. O E	E r?		0	
He ca	rries out an cords the re E	experiments as E of E o	nt by rolling (even) or the oreal of the ore	ng the d O (odd) E an ever	ice. O E n numbe	E r?	ОЕ	0	
Не са Не гес (а) V	rries out an cords the re  E What is the 1	experiments as E of E o	ove the exp	ng the d O (odd) E San ever	ice. O E n numbe	E r?	O E	0	

1. (a) All 16 scores correct

A2 (A1 for 12 correct)

**(b)**  $\frac{11}{36}$ 

A1 (for identifying 11), A1 (for correct answer)

2.

(a)	3	5	7	9	11	13
	5	7	9	11	13	15
	7	9	11	13	15	17

A2

**(b)**  $\frac{6}{18}$  or  $\frac{1}{3}$ 

M1 A1

3.

(a)

2, 3

3, 2 3, 3

4, 1

4, 2 4, 3

A1

**(b)**  $\frac{3}{12}$   $\left(\frac{1}{4}\right)$  (0.25)

A1

(c)  $\frac{6}{12}$   $\left(\frac{1}{2}\right)$  (0.5)

(a)		Box 2				
		1	2	3	4	
	2	(2, 1)	(2, 2)	(2, 3)	(2, 4)	
Box 1	4	(4, 1)	(4, 2)	(4, 3)	(4, 4)	
	5	(5, 1)	(5, 2)	(5, 3)	(5, 4)	

Allow A1 for 8 correct

A2

**(b)** 
$$\frac{2}{12} \left( \frac{1}{6} \right)$$

A1

(c) 
$$\frac{10}{12} \left( \frac{5}{6} \right)$$

A1

(d) using 
$$\frac{1}{6}$$

A1

$$\frac{1}{6} \times 30 = 5$$

M1 A1

5. **(a)** 
$$0.8 \text{ (or } \frac{4}{5})$$

A1

MA2

(a)		(G, H)	(B, H)	(W, H)	(Y, H)
	(R, T)	(G, T)	(B, T)	(W, T)	(Y, T)

M1 A1

(b)  $\frac{1}{10}$  (c)  $\frac{6}{10}$ 

A1

M1 A1

7. (a)

	1	3	5	7	9
1	2	4	6	8	10
3	4	6	8	10	12
5	6	8	10	12	14
7	8	10	12	14	16
9	10	12	14	16	18

18 correct A2 At least 12 correct A1

**(b)** 
$$\frac{5}{25} \left(\frac{1}{5}\right)$$

(a) Head Blue, Head Red, Head Yellow, Head Green Tail Blue, Tail Red, Tail Yellow, Tail Green

8 correct A2 At least 6 correct A1

**(b)** There are 8 outcomes

One outcome is Tail Yellow

**A**1

$$\left( P \left( \text{Tail Yellow} \right) = \frac{1}{8} \right)$$

9.

(a) 10 correct missing pairs added to table

H2 H3 H4 H5 H6

T1 T2 T3 T4 T6

(at least 6 correct A1)

Δ1

**(b)** 
$$\frac{2}{12}$$
 or  $\frac{1}{6}$ 

A1

(c) 
$$\frac{3}{12}$$
 or  $\frac{1}{4}$ 

**A**1

10.

SP, SB, SC, SQ MP, MB, MC, MQ RP, RB, RC, RQ

M1

12

**11**. **(a)** 10, 20, 30, 40

20, 40, 60, 80

30, 60, 90, 120 (allow A1 for at least 6 correct)

MA2

**(b)**  $\frac{2}{12}$  or equivalent

A1

(c)  $\frac{5}{12}$ 

M1 A1

12.

(a) 16 black, 16 red, 16 yellow, 16 green 64 black, 64 red, 64 yellow, 64 green

A2 (A1 for 5 correct)

**(b)**  $\frac{1}{8}$ 

A1

13.

	1	2	3	4	5	6
	H1					
T	T1	T2	T3	T4	T5	T6
$\frac{1}{12}$						

M1

$$1+6$$
,  $2+5$ ,  $3+4$ ,  $4+3$ ,  $5+2$ ,  $6+1$ 

A2 (A1 for 3 correct)

15.

C A B

A1 A1 A1

16.

(a) V indicated at 0.2

A1

**(b)** M indicated at 0.6

A1

17.

(a) 🗸

A1

(b) •

**A**1

(c) X

**A**1

(d) \*

18. B at 0.2 W at 0.5 R at 0

A1 A1 A1

19. (a) X at or very near to zero

A1

**(b)** X at 1

A1

(c) X at 0.5

A1

(d) 30% (or equivalent)

A1

20.

(a) It is certain to happen

A1

**(b)** An arrow marked at 0

A1

(c) Half of the tickets may not be bought by boys

A1

21.

(a) (i) G at zero

A1

(ii) 
$$\frac{7}{8}$$
 written

MA1

(ii)  $\frac{7}{8}$  written
T correctly positioned at  $\frac{7}{8}$  on scale

A1

**(b)** 4 reds = 
$$\frac{1}{5}$$
, so 20 counters

MA1

12 pink counters

MA1

22.	<ul><li>(a) It is not possible to have a probability greater than 1</li><li>(b) 0.74</li></ul>	A1 A1
23.	No because although there are an equal number of circles and triangles them still have less chance than the squares which have a probability of (or no; the probability of choosing a triangle is 0.25 as there are only 2 a total of 8) (or equivalent)	of $\frac{1}{2}$
24.	(a) A (b) C	A1 A1
25.	<ul><li>(a) C</li><li>(b) B</li><li>(a) A</li></ul>	A1 A1 A1

(a) 
$$\frac{15}{21} \left( \frac{5}{7} \right)$$

A1

**(b)** 
$$\frac{7}{21} \left( \frac{1}{3} \right)$$

A1

27.

**(a)** 28

A1

**(b)**  $\frac{10}{28}$   $\left(\frac{5}{14}\right)$ 

A1

(c)  $\frac{10}{14}$   $(\frac{5}{7})$ 

M1 A1

28.

- (a)  $\frac{4}{6} \left( \frac{2}{3} \right)$  (b) 0 (c)  $\frac{1}{6}$

A1 for each

29. 400 - 275 = 125

MA1

 $\frac{125}{400}$ 

$$0.28 + 0.12 + 0.09$$
  
 $0.49$ 

(a) 
$$\frac{11}{14}$$

**(b)** 
$$\frac{3}{13}$$

32. 1 - (0.3 + 0.4) = 0.3 $0.3 \div 2 = 0.15$ 

33.

(a) 
$$\frac{1}{81}$$

**(b)** 
$$\frac{11}{81}$$

(c) not an equal number of odd and even

(a) 7 pupils picked different colours (or some don't have favourite colour)

A1

**(b)**  $\frac{5}{18}$ 

**A**1

(c)  $\frac{25}{32}$ 

A1

35.

(a)  $\frac{9}{100}$  (0.09)

A1

**(b)**  $\frac{9}{100} \times 5000 = 450$ 

M1 A1

36.

(a)  $\frac{8}{24}$  separate marks for numerator, denominator correct

A1 A1

**(b)**  $\frac{10}{24}$ 

A1

(c) Yes because it was  $\frac{5}{24}$  and is now  $\frac{5}{25}$ 

MA1 MA1

or total number of pupils has changed but number of girls wearing glasses has not (following YES)

MA1 MA1

(a)	5
(a)	8

**A**1

A1

**(b)** Not a valid conclusion as he has not made enough trials to support this

38.

(a) 0.34 × 200 68

M1 A1

(b) 0.32
Because more spins means that it is more reliable

A1 A1

39.

(a)  $300 \times 0.27$ 

M1

81

**A**1

**(b)** 0.25

A1

The bigger the sample size the more reliable is the estimate

**A**1

(c)  $300 \times \frac{1}{6}$ 

M1

50

**(a)** 0.38

A1

**(b)** 27

A1

(c) YES you expect D about 15 times or rel freq should be 0.25

A1 A1

(d)  $400 \times 0.45 = 180$ 

M1 A1

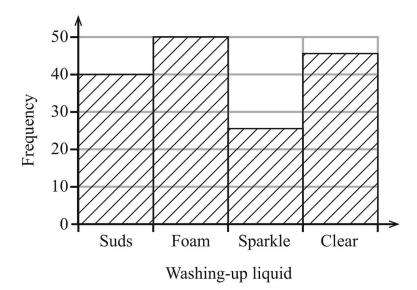
41.

(a)  $\frac{7}{12}$ 

**A**1

**(b)** By increasing the number of trials.

Q1 A survey was carried out in a supermarket to find which washing-up liquid people buy.



(a) A customer is chosen at random. What is the probability that they buy either Foam or Sparkle?

Answer	[2]

**(b)** The supermarket is ordering new stock. They are going to order 8000 bottles in total. Based on the results of this survey, how many bottles of Clear should they order?

Answer \_\_\_\_\_ [2]

Q2 Bobby the builder has nails of five different lengths in a jar.

The probability of a nail being a certain length is given in the table.

Length (mm)	20	24	30	36	44
Probability	0.15		0.2	0.25	0.35

(a)	What is	the prob	ability of	`a nail	being 24 mm	long
-----	---------	----------	------------	---------	-------------	------

Answer		[2]
--------	--	-----

There are 60 nails in the jar.

**(b)** How many nails are longer than 30 mm?

Answer \_\_\_\_\_ [3]

Q3	A bag	contains	only red,	blue.	vellow	and	white	counters
Y-		O LI COLLIS	O ,	~~~,	,		, ,	O CHILDER

The table shows the probability of taking some of these colours from the bag at random.

Colour	red	blue	yellow	white
Probability	0.2	0.35		0.3

(a) '	Work out	the	probability	of taking	a yellow	counter	from	the b	oag.
-------	----------	-----	-------------	-----------	----------	---------	------	-------	------

Answer	[:	2

**(b)** The bag contains a total of 1500 counters.

How many blue counters would you expect the bag to contain?

Answer	[2]
Answer	 [2

There are four possible results from a music examination.

Result	Fail	Pass	Credit	Distinction
Probability		$\frac{1}{2}$	$\frac{3}{10}$	$\frac{1}{20}$

The probabilities of some results are recorded in the table.

(a) What is the probability of fail?

Answer		[2]	1

**(b)** What is the probability of credit or distinction?

Answer	[2]	
--------	-----	--

(		5
◟	Į	J

A box contains sweets.

The sweets are strawberry, lime, orange or blackcurrant flavour.

A sweet is taken at random from the box.

The table below shows some of the probabilities.

Flavour	strawberry	lime	orange	blackcurrant
Probability	0.45			0.25

(a)	The box	has an equal	l number of	lime and	orange sweets.
-----	---------	--------------	-------------	----------	----------------

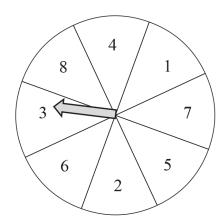
Work out the probability that an orange sweet will be taken.

Answer	[2]
	12

**(b)** The box contains a total of 120 sweets.

How many strawberry sweets should it contain?

Answer	[2]



A spinner consists of a circular wheel which is divided into eight sectors numbered 1 to 8 as in the diagram.

When spun, the arrow will point to one of the sectors.

(a)	What is	meant	if the	spinner	is	described	as	a fair	spinne	er?
-----	---------	-------	--------	---------	----	-----------	----	--------	--------	-----

Answer			
			[1]

**(b)** The spinner is **not** fair.

The probability of the arrow pointing to the sector numbered 7 is 0.15

Work out the probability of the arrow not pointing to the sector numbered 7

A	
Answer	7

•		
(	) [	

In a herd of 40 goats there are

8 brown 9 white 13 without horns

A goat is taken at random from the herd.

What is the probability that this goat

(a) has horns,



Answer \_\_\_\_\_ [1]

**(b)** is brown or white,

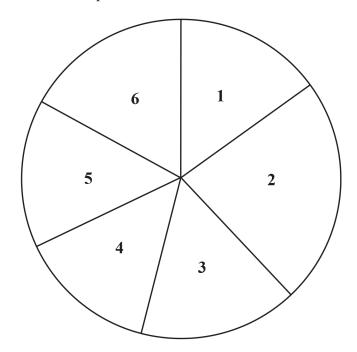
Answer \_\_\_\_\_ [1]

(c) is not brown or white?

Answer \_\_\_\_\_ [1]

Georgia rolls a dice a number of times and records the outcome each time.

She displays her results in this pie chart.



Alice thinks Georgia's dice is biased.

Bob disagrees.

What information is needed to decide who is correct?

Answer		[1	ľ
--------	--	----	---

Visitors to Northern Ireland were asked to name their favourite tourist attraction.

The table of probabilities is based on their responses.

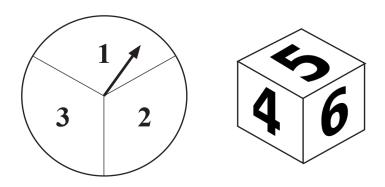
Estimate how many named Giant's Causeway.

Tourist attraction	Giant's Causeway	Ulster Museum	Titanic Belfast	Mussenden Temple	Derry City Walls	Other
Probability	0.3	0.1	0.14			0.2

The probability of Mussenden Temple is the same as the probability of Derry City Walls.

(a)	Complete the table.	[3]
(b)	What is the probability a visitor named Ulster Museum or Titanic Belfast?	
	Answer	[1]
(c)	Last week 1800 visitors were asked to name their favourite tourist attraction.	

Answer [2]



The fair spinner shown is spun and a fair dice is thrown.

The number the spinner lands on is added to the number on the dice to give a total score.

Complete the table of total scores.

		Dice					
		1	2	3	4	5	6
	1	2	3	4	5		
pinner	2	3	4	5			
	3	4	5				

Sp

What is the probability of a total score of 4?

Answer	 [1	]

[2]

What is the probability of a total score greater than or equal to 5?

Answer	Γ1	l



© Getty Images

Answer \_\_\_\_\_ [2]

When Susan goes to the cinema, she always buys only one item.

She buys a drink or popcorn or crisps or ice cream.

Some of the probabilities are shown.

Item	Probability
A drink	0.4
Popcorn	0.15
Crisps	
Ice cream	0.2

Work out the probability that Susan buys crisps.

Susan goes to the cinema 20 times.	
Calculate how many times you would expect her to buy a drink.	
Answer	[2]
Allswei	[∠]

Q12 In a group, the number of boys and girls with a certain eye colour is recorded as shown below.

	Boys	Girls
Brown eyes	10	8
Blue eyes	4	7
Green eyes	6	5

A child is chosen at random from this group of boys and girls.

What is the probability that the child is a girl with blue eyes?

Answer	[2]
	1-

SET A			SET B	
2 4	6	1	3	5

A card is taken at random from Set A.

A card is then taken at random from Set B.

The cards are used to make a two-digit number in the order AB.

what is the probability that the two-digit humber

(i) is even,

Answer \_\_\_\_\_ [1]

Complete

1 kg is approximately equal to \_\_\_\_\_\_ lbs

[1]

Q14 Data is recorded about the age and treatment received by patients who visit a dentist on a Monday.

	Patients aged 30 or under	Patients aged over 30	
Filling	9	6	
Extraction	5	13	

		Extraction	5	13	
(a)		ne probability than extraction?	at one of these patient	es selected at random	is over 30
				Answer	[1]
(b)	One of the	e patients aged 3	0 or under is selected	at random.	
	What is th	ne probability that	at this patient has a fi	lling?	

Ben observes whether cars turn right or left at a T junction. He records the number of cars that come to the junction and the number that turn left.

Number of cars observed	10	20	50	100
Number of cars that turn left	4	13	33	72

(a)	What is the relative	frequency of cars	turning left after	50 observations?
-----	----------------------	-------------------	--------------------	------------------

Answer	Γ1	1
	_ ~	

**(b)** What is the best estimate for the probability that a car will turn left at this junction?

Answer [	1	1	

(c) In one week 580 cars come to this junction.

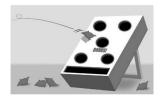
Estimate how many turn **right**.

Answer	[2]

Q16	A company makes memory chips.
	The probability that one of these memory chips is faulty is 0.025
	The company makes 1800 memory chips each hour.
	Work out an estimate for the number of memory chips made per hour that will <b>not</b> be faulty.
	Answer [3]

Q17 Kate plays the game "throw the bean bag".

She records the number of times she gets the bean bag in the bonus hole.



Total number of throws	10	30	100	200
Total number of times in the bonus hole	2	8	49	104

		the bonus hole	2	8	49	104	
(a)	bon	ite down the best estimate on the hole if she continues throws a reason for your answer.	owing.	bility that k	Kate gets th	e bean bag	in the
		swer					
	bec	ause					[2]
(b)	Kat	te continues with her game	and throws	it a total of	`300 times.		
		culate the number of times nus hole.	you would	expect her	to get the b	ean bag in	the
					Answer _		[2]

A survey is carried out to find out the number of electric cars on the road.

One hundred cars are surveyed each day for four days.

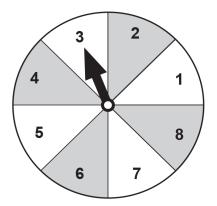
The results are recorded in the following table along with the relative frequencies so far.

Day	Number of cars surveyed	Number of electric cars	Relative frequency
1	100	11	0.11
2	100	12	0.115
3	100	16	0.13
4	100	9	

(a) Work out the missing relative frequency and reco	ord it in the table. [1]
--	--------------------------

<b>(b)</b>	What would be the best estimate for the probability that a car chosen at random
	is electric?

Answer	[1]



The spinner is spun 1000 times.

The table shows some of the number of times it landed on the number 3 and some of the calculated relative frequency values.

Number of spins	Number of threes	Relative frequency
20	2	0.1
200	26	0.13
500	64	
1000		0.122

Calculate the missing relative frequency value.

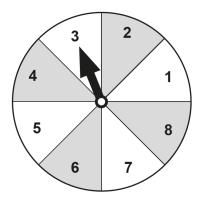
Answer	[1]

Calculate the number of times it landed on a 3 for the 1000 spins.

Answer	Г1	1
1 1115 11 01	L^	J

Use the best relative frequency value from the table to calculate the number of threes you would expect to get in 2500 spins.

swer [2]
swer [2



The spinner is spun 1000 times.

The table shows some of the number of times it landed on the number 3 and some of the calculated relative frequency values.

Number of spins	Number of threes	Relative frequency
20	2	0.1
200	26	0.13
500	64	
1000		0.122

		Calavilata	the mi	a a i m a m	alatirra	fraguana	
(	$\mathbf{a}$	Calculate	me iiii	ssing re	eialive.	rrequency	y varue.

Answer	Γ1 <b>1</b>
Allowel	1 1

**(b)** Calculate the number of times it landed on a 3 for the 1000 spins.

Answer	Γ.	17	
AH3WCI			

(c) Use the best relative frequency value from the table to calculate the number of threes you would expect to get in 2500 spins.

Answer	12.1

Q21	(a)	When a spinner was spun 50 times, it landed on red 12 times. When spun another 50 times, it landed on red another 9 times.				
		Cal	culate the relative frequency for red			
		(i)	after the first 50 spins,			
			Answer [1	.]		
		(ii)	after the 100 spins.			
			Answer [1	.]		
	(b)	The spinner landed on yellow 40 times in the 100 spins.				
		(i)	Estimate the probability for this spinner landing on yellow.			
			Answer [1	]		
		(ii)	Estimate how many times the spinner will land on yellow in 300 spins.			
			Answer [1	]		

1. **(a)** Total of 75 or 76 MA1 
$$\frac{75}{160}$$
 (or  $\frac{15}{32}$ ) or  $\frac{76}{162}$  (or  $\frac{38}{81}$ ) or  $\frac{75}{161}$  or  $\frac{76}{161}$  MA1

**(b)** 
$$\frac{45}{160} \times 8000$$
 or  $\frac{46}{162} \times 8000$  or  $\frac{45}{161} \times 8000$  or  $\frac{46}{161} \times 8000$  M1  
= 2250 or 2272 or 2236 or 2285 or 2286 or 2271

2. **(a)** 
$$1 - (0.15 + 0.2 + 0.25 + 0.35) = 0.05$$
 M1, A1  
**(b)**  $0.6 \times 60 = 36$  A1, M1, A1

3. **(a)** 
$$1 - (0.2 + 0.35 + 0.3)$$
 M1  $0.15$  M1 **(b)**  $1500 \times 0.35$  M1  $525$  M1

4

(a) 
$$1 - \left(\frac{1}{2} + \frac{3}{10} + \frac{1}{20}\right) = \frac{3}{20}$$

M1 A1

**(b)** 
$$\frac{3}{10} + \frac{1}{20} = \frac{7}{20}$$

M1 A1

5.

(a) 
$$1 - 0.45 - 0.25 = 0.3$$
  
 $0.3 \div 2 = 0.15$ 

MA1 A1

M1 A1

6.

(a) Each number has an equal chance / each sector is the same size

A1

M1

0.85

(a) 
$$\frac{27}{40}$$

A1

**(b)** 
$$\frac{17}{40}$$

A1

(c) 
$$\frac{23}{40}$$

A1

8.

number of trials

A1

9.

(a) 
$$0.3 + 0.1 + 0.14 + 0.2 = 0.74$$

MA1

$$1 - 0.74 = 0.26$$

MA1

$$0.26 \div 2 = 0.13$$
; 0.13 and 0.13

MA1

**(b)** 0.24

**A**1

(c) 
$$0.3 \times 1800 = 540$$

M1A1

(a)		1	2	3	4	5	6
	1	2	3	4	5	6	7
	2	3	4	5	6	7	8
	3	4	5	6	7	8	9

A2

6 correct for [1] 9 correct for [2]

**(b)** 
$$\frac{3}{18} \left( \frac{1}{6} \right)$$

A1

(c) 
$$\frac{12}{18} \left( \frac{2}{3} \right)$$

A1

11.

M1

$$= 0.25$$

A1

**(b)** 
$$20 \times 0.4 = 8$$

M1 A1

12.

MA1

$$\frac{7}{40}$$

(a) 21 23 25 41 43 45 61 63 65

M1 A1

(i) 0 or impossible

A1

(ii)  $\frac{3}{9} \left(\frac{1}{3}\right)$ 

**A**1

14.

(a)  $\frac{13}{33}$ 

A1

**(b)**  $\frac{9}{14}$ 

A1

15.

(a)  $\frac{33}{50}$  (0.66)

A1

**(b)**  $\frac{72}{100}$  (0.72)

A1

(c)  $580 \times 0.28 = 162.4 = 162 \text{ cars}$ 

M1 A1

16.

1 - 0.025 = 0.975 or  $1800 \times 0.025 = 45$   $1800 \times 0.975$  or 1800 - 451755 1755 MA1 M1 A1

(a) 
$$\frac{104}{200} \left(\frac{13}{25}\right) (0.52)$$

A1

The more throws the better the probability estimate

**A**1

**(b)** 
$$\frac{104}{200} \times 300 = 156$$

M1 A1

18.

(a) 0.12

A1

**(b)** 0.12

A1

19.

(a) 
$$\frac{64}{500} = 0.128$$

MA1

**(b)** 
$$1000 \times 0.122 = 122$$

MA1

(c) 
$$2500 \times 0.122$$

M1

(a) 
$$\frac{64}{500} = 0.128$$

MA1

**(b)** 
$$1000 \times 0.122 = 122$$

MA1

(c) 
$$2500 \times 0.122$$

M1

$$= 305$$

A1

21.

(a) (i)  $\frac{12}{50}$  or equivalent

A1

(ii)  $\frac{21}{100}$  or equivalent

A1

**(b)** (i)  $\frac{40}{100}$  or equivalent

A1

(ii) 120